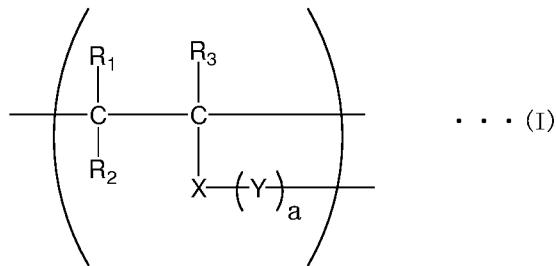


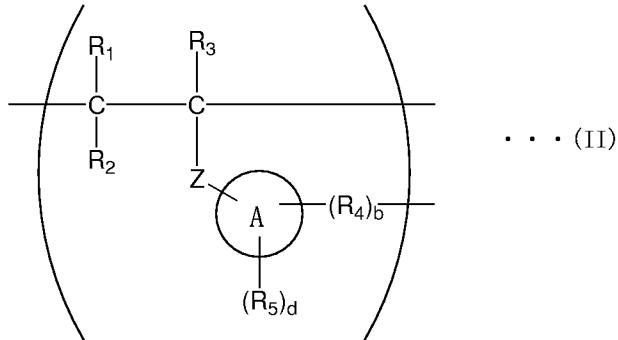
CLAIMS

1. A multi-branched polymer having repeating units represented by a formula (I):



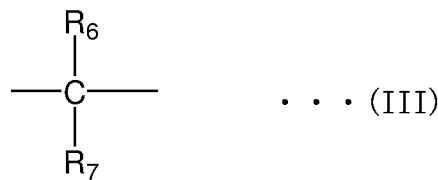
5 wherein R_1 to R_3 each independently represents hydrogen or a hydrocarbon group, R_1 may be bonded to R_3 to form a ring; X represents a connecting group having a valence of 3 or higher; Y may be the same or different and each represents a functional group which may have an active halogen atom; and a is an integer of 2 or larger.

2. The multi-branched polymer according to claim 1, wherein the repeating units
10 represented by the formula (I) are repeating units represented by a formula (II):



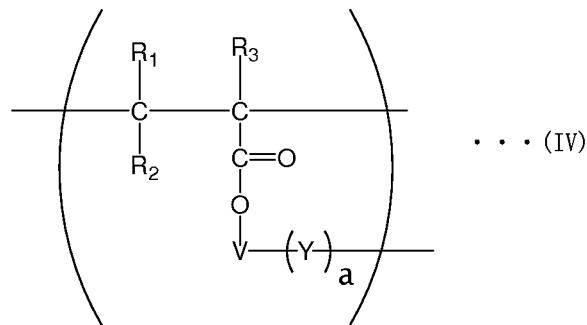
wherein R_1 to R_3 are as defined above; Z represents a single bond or a connecting group having a valence of 2 or higher; A represents an aromatic hydrocarbon group or an aromatic heterocyclic group; R_4 may be the same or different and each represents a functional group which may have an active halogen atom; b is an integer of 2 or larger; R_5 represents a halogen atom or an organic group and d is 0 or an integer of 1 or larger and R_5 may be the same or different when d is 2 or larger.

3. The multi-branched polymer according to claim 2, wherein in the formula (II), Z is a single bond; A is an aromatic hydrocarbon ring; and R₄ is a functional group represented by a formula (III):



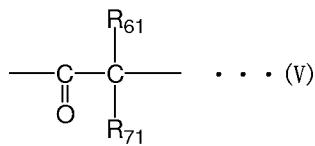
5 wherein R₆ and R₇ each independently represents hydrogen, a halogen atom, an alkyl group which may have a substituent, or a linkage with other repeating units with a proviso that R₆ and R₇ do not become linkages with other repeating units at the same time.

4. The multi-branched polymer according to claim 1, wherein the repeating units 10 represented by the formula (I) are repeating units represented by a formula (IV):



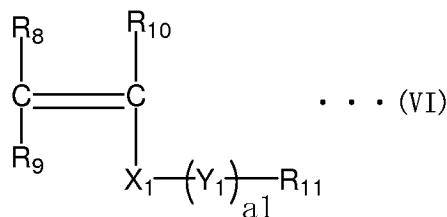
wherein R₁ to R₃, Y, and a are as defined above; and V represents a connecting group having a valence of 3 or higher.

15 5. The multi-branched polymer according to claim 4, wherein V is a polyoxyalkylene group in the formula (IV).
 6. The multi-branched polymer according to claim 4 or 5, wherein in the formula (IV), Y is a functional group represented by a formula (V):



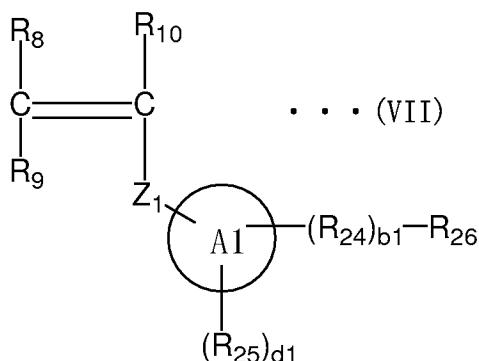
wherein R_{61} and R_{71} each independently represents hydrogen, a halogen atom, an alkyl group which may have a substituent, or a linkage with other repeating units with a proviso that R_{61} and R_{71} do not become linkages with other repeating units at the same time.

7. A multi-branched polymer obtained with a living radical polymerization method using a metal catalyst by polymerizing compounds represented by a formula (VI):



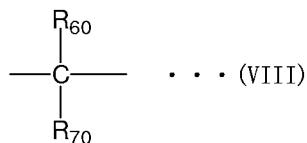
10 wherein R_8 to R_{10} each independently represents hydrogen or a hydrocarbon group, and R_8 may be bonded to R_{10} to form a ring; X_1 represents a connecting group having a valence of 3 or higher; Y_1 may be the same or different and each represents a functional group which may have an active halogen atom; $a1$ is an integer of 2 or larger; and R_{11} represents a chlorine atom, a bromine atom, or an iodine atom.

15 8. The multi-branched polymer according to claim 7, wherein the compounds represented by the formula (VI) are compounds represented by a formula (VII):



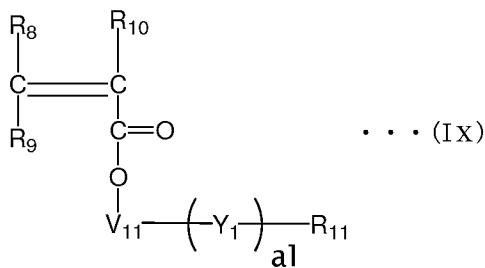
wherein R₈ to R₁₀ are as defined above; Z₁ represents a single bond or a connecting group having a valence of 2 or higher; A1 represents an aromatic hydrocarbon group or an aromatic heterocyclic group; R₂₄ may be the same or different and each represents a functional group which may have an active halogen atom; b1 is an integer of 2 or larger; R₂₅ represents a halogen atom or an organic group and d1 is 0 or an integer of 1 or larger and R₂₅ may be the same or different when d1 is 2 or larger; R₂₆ represents a chlorine atom, a bromine atom, or an iodine atom.

9. The multi-branched polymer according to claim 8, wherein in the formula (VII), Z₁ is a single bond, A1 is an aromatic hydrocarbon group, and R₂₄ is a functional group represented by a formula (VIII):



wherein R₆₀ and R₇₀ each independently represents hydrogen, a halogen atom, or a C1 to C6 alkyl group which may have a substituent with a proviso that R₆₀ and R₇₀ are not halogen atoms other than fluorine atoms at the same time.

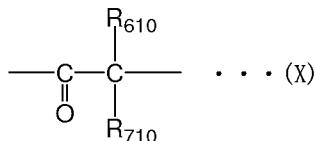
10. The multi-branched polymer according to claim 7, wherein the compounds represented by the formula (VI) are compounds represented by a formula (IX):



wherein R_8 to R_{10} are as defined above respectively; V_{11} represents a connecting group having a valence of 3 or higher; Y_1 may be the same or different and each represents a functional group which may have an active halogen atom; $\text{a}1$ is an integer of 2 or larger; and R_{11} represents a chlorine atom, a bromine atom, or an iodine atom.

11. The multi-branched polymer according to claim 10, wherein V_{11} is a polyoxyalkylene group in the formula (IX).

12. The multi-branched polymer according to claim 10 or 11, wherein in the formula (IX), Y_1 is a functional group represented by a formula (X):



wherein R_{610} and R_{710} each independently represents hydrogen, a halogen atom, an alkyl group which may have a substituent, or a linkage with other repeating units with a proviso that R_{610} and R_{710} do not become linkages with other repeating units at the same time.

13. The multi-branched polymer according to claim 1 or 7, wherein a ratio (Mw/Mn) of weight average molecular weight (Mw) to number average molecular weight (Mn) of the polymer is in a range between 1.01 and 9.99.

20 14. The multi-branched polymer according to claim 1 or 7, wherein the number average molecular weight (Mn) of the polymer is in a range between 200 and 20,000,000.

15. The multi-branched polymer according to claim 1 or 7, wherein the multi-branched polymer is a hyperbranched polymer.

16. A hyperbranched polymer which is branched by a carbon-carbon bond and has a ratio (Mw/Mn) of weight average molecular weight (Mw) to number average molecular weight (Mn) in a range between 1.01 and 9.99.

5 17. A hyperbranched polymer obtained by polymerizing a compound having 2 or more polymerization-initiation sites and polymerizable unsaturated bonds by a living radical polymerization method using a metal catalyst.

18. The hyperbranched polymer according to claim 16 or 17, wherein the number 10 average molecular weight (Mn) of the polymer is in a range between 200 and 20,000,000.

19. The hyperbranched polymer according to claim 16 or 17, wherein the polymer has a functional group at a polymer terminal.

20. A star polymer having the multi-branched polymer according to claim 1 or 7 or the

15 hyperbranched polymer according to claim 16 or 17 as a core thereof.